

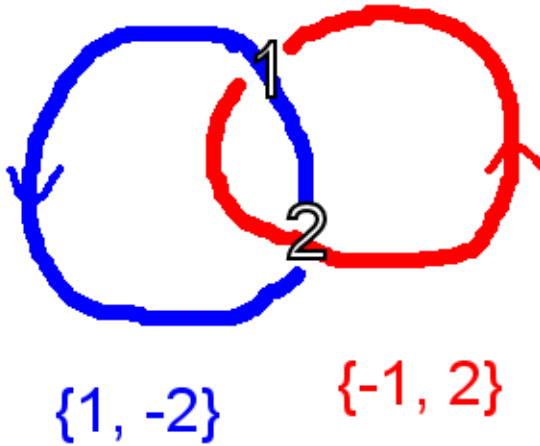
(Directory and \$Path initialization not included.)

`Needs ["KnotTheory`"]`

Loading KnotTheory` version of September 6, 2014, 13:37:37.2841.  
 Read more at <http://katlas.org/wiki/KnotTheory>.

A simple link, albeit with ambiguous orientation:

`hopfGC = {{1, -2}, {2, -1}};`



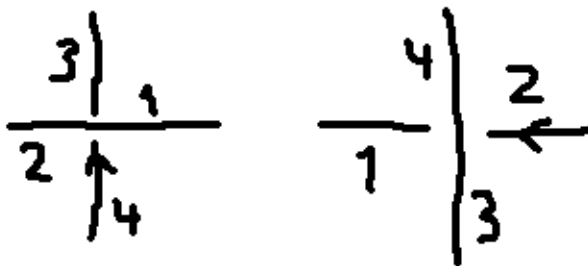
I ask for its planar diagram:

`hopfPD = PD[GaussCode @@ hopfGC]`

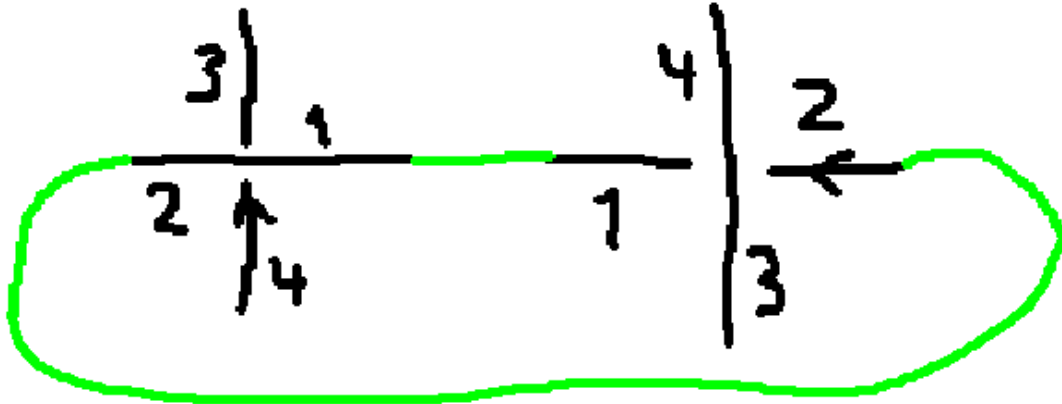
KnotTheory::credits : The GaussCode to PD conversion was written by Siddarth Sankaran at the University of Toronto in the summer of 2005.

`PD[X[4, 1, 3, 2], X[2, 4, 1, 3]]`

But that's impossible. Here are those crossings...



... and I try to connect them ...



... but 3 and 4 are trapped on opposite sides.

DrawMorseLink finds out:

**DrawMorseLink [hopFPD]**

KnotTheory::credits : MorseLink was added to KnotTheory` by Siddarth Sankaran at the University of Toronto in the summer of 2005.

Part::partw : Part 3 of Knot[MorseLink::Error: bad input] does not exist. >>

Part::partw : Part 2 of Knot[MorseLink::Error: bad input] does not exist. >>

Part::partw : Part 4 of Knot[MorseLink::Error: bad input] does not exist. >>

General::stop : Further output of Part::partw will be suppressed during this calculation. >>

\$Aborted

Jones doesn't panic, just gives wrong stuff:

**Factor [Jones [hopFPD] [t]]**

$$\frac{1+t}{\sqrt{t}}$$

Same link, in hopes of coaxing:

**hopFGC2 = {{1, -2}, {-1, 2}};**

Still wrong:

**hopFPD2 = PD[GaussCode @@ hopFGC2]**

PD[X[3, 2, 4, 1], X[2, 4, 1, 3]]

**DrawMorseLink [hopFPD2]**

Part::partw : Part 3 of Knot[MorseLink::Error: bad input] does not exist. >>

Part::partw : Part 2 of Knot[MorseLink::Error: bad input] does not exist. >>

Part::partw : Part 4 of Knot[MorseLink::Error: bad input] does not exist. >>

General::stop : Further output of Part::partw will be suppressed during this calculation. >>

\$Aborted

Jones is still wrong, but different.

```
Factor [Jones [hopfPD2] [t]]
```

$$-t (1 + t)$$

But isn't the Hopf link in the big list?

```
AllLinks [2, Alternating]
```

```
{Link [2, Alternating, 1]}
```

```
hopf0 = Link [2, Alternating, 1]
```

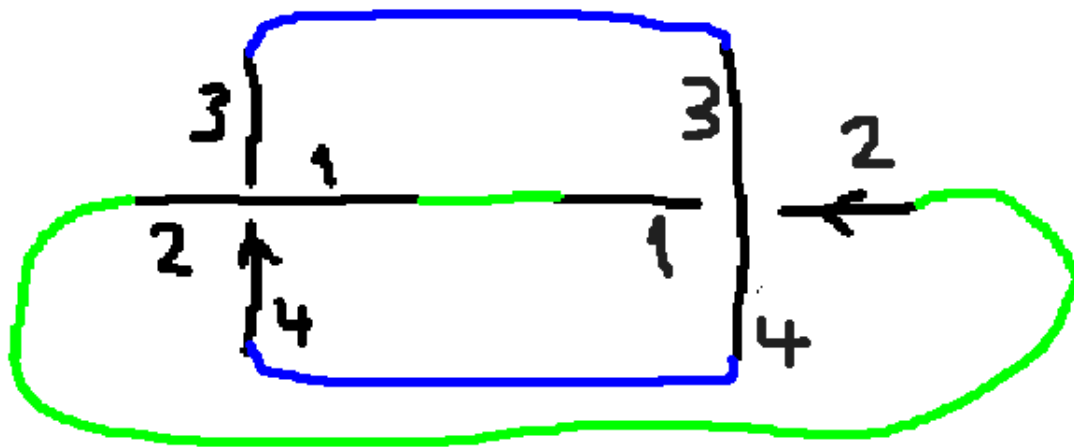
```
Link [2, Alternating, 1]
```

This is good, but perhaps only because it was precomputed...

```
PD [hopf0]
```

KnotTheory::loading : Loading precomputed data in PD4Links`.

```
PD [X [4, 1, 3, 2], X [2, 3, 1, 4]]
```



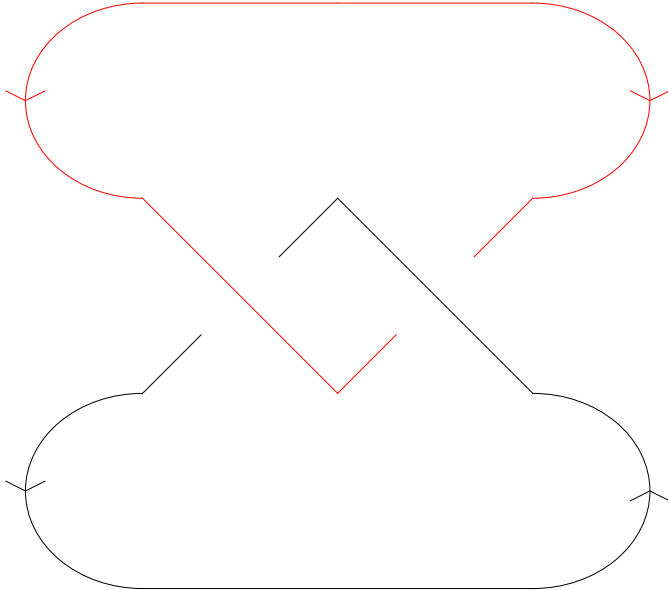
... and this looks okay, until you realize we saw it before.

```
GaussCode [hopf0]
```

```
GaussCode [ {1, -2}, {2, -1} ]
```

Nice picture ... until you follow the orientation! (Two praying mantises locked in a death-kiss?)

**DrawMorseLink [hopf0]**



This was run in Mathematica 10, but the same sorts of things were present in 9 (and even 8, I believe). The same behavior occurs in a “version of March 22, 2011, 21:10:4.67737”.

Other trivial links suffer similarly. Two overlapping unlinked components can even produce the same impossible planar diagram:

**PD[GaussCode[{1, 2}, {-1, -2}]]**

PD[X[3, 2, 4, 1], X[4, 1, 3, 2]]

**PD[GaussCode[{1, -2}, {-1, 2}]]**

PD[X[3, 2, 4, 1], X[2, 4, 1, 3]]